

## DERIVATIVES

function	derivative
$x^n$	$nx^{n-1}$
$e^x$	$e^x$
$a^x (a > 0)$	$a^x \ln a$
$\ln x$	$\frac{1}{x}$
$\log_a x$	$\frac{1}{x \ln a}$
$\sin x$	$\cos x$
$\cos x$	$-\sin x$
$\tan x$	$\sec^2 x$
$\operatorname{cosec} x$	$-\operatorname{cosec} x \cot x$
$\sec x$	$\sec x \tan x$
$\cot x$	$-\operatorname{cosec}^2 x$
$\sin^{-1} x$	$\frac{1}{\sqrt{1-x^2}}$
$\cos^{-1} x$	$-\frac{1}{\sqrt{1-x^2}}$
$\tan^{-1} x$	$\frac{1}{1+x^2}$
$\sinh x$	$\cosh x$
$\cosh x$	$\sinh x$
$\tanh x$	$\operatorname{sech}^2 x$
$\operatorname{cosech} x$	$-\operatorname{cosech} x \coth x$
$\operatorname{sech} x$	$-\operatorname{sech} x \tanh x$
$\coth x$	$-\operatorname{cosech}^2 x$
$\sinh^{-1} x$	$\frac{1}{\sqrt{1+x^2}}$
$\cosh^{-1} x (x > 1)$	$\frac{1}{\sqrt{x^2-1}}$
$\tanh^{-1} x ( x  < 1)$	$\frac{1}{1-x^2}$
$\coth^{-1} x ( x  > 1)$	$-\frac{1}{x^2-1}$

Product Rule

$$\frac{d}{dx}(u(x) v(x)) = u(x) \frac{dv}{dx} + v(x) \frac{du}{dx}$$

Quotient Rule

$$\frac{d}{dx} \left( \frac{u(x)}{v(x)} \right) = \frac{v(x) \frac{du}{dx} - u(x) \frac{dv}{dx}}{[v(x)]^2}$$

Chain Rule

$$\frac{d}{dx} (f(g(x))) = f'(g(x)) \times g'(x)$$

Leibnitz's theorem

$$\frac{d^n}{dx^n} (f \cdot g) = f^{(n)} \cdot g + n f^{(n-1)} \cdot g^{(1)} + \frac{n(n-1)}{2!} f^{(n-2)} \cdot g^{(2)} + \dots + \binom{n}{r} f^{(n-r)} \cdot g^{(r)} + \dots + f \cdot g^{(n)}$$